## Notation and Symbols

| $\mathbb{R}$ | the set of reals |
| :---: | :---: |
| $\mathbb{N}$ | the set of natural numbers, $\mathbb{N}=\{1,2, \ldots\}$ |
| $x$ | the input domain |
| $N$ | (used if $X$ is a vector space) dimension of $X$ |
| $x_{i}$ | input patterns |
| $y_{i}$ | target values $y_{i} \in \mathbb{R}$, or (in pattern recognition) classes $y_{i} \in\{ \pm 1\}$ |
| m | number of training examples |
| [ $m$ ] | compact notation for $\{1, \ldots, m\}$ |
| $i, j$ | indices, by default running over [ m ] |
| X | a sample of input patterns, $X=\left(x_{1}, \ldots, x_{m}\right)$ |
| $Y$ | a sample of output targets, $Y=\left(y_{1}, \ldots, y_{m}\right)$ |
| $\mathcal{H}$ | feature space |
| $\Phi$ | feature map, $\Phi: \mathcal{X} \rightarrow \mathcal{H}$ |
| $\mathrm{x}_{i}$ | a vector with entries $\left[\mathbf{x}_{i}\right]_{j}$; usually a mapped pattern in $\mathcal{H}, \mathbf{x}_{i}=\Phi\left(x_{i}\right)$ |
| w | weight vector in feature space |
| b | constant offset (or threshold) |
| k | (positive definite) kernel |
| K | kernel matrix or Gram matrix, $\mathrm{K}_{i j}=k\left(x_{i}, x_{j}\right)$ |
| E[ ${ }^{\text {] }}$ | expectation of a random variable $\xi$ (Section B.1.3) |
| P $\{\cdot\}$ | probability of a logical formula |
| $\mathrm{P}(\mathrm{C})$ | probability of a set (event) C |
| $p(x)$ | density evaluated at $x \in \mathcal{X}$ |
| $\mathcal{N}(\varepsilon, \mathcal{F}, d)$ | covering number of a set $\mathcal{F}$ in the metric $d$ with precision $\varepsilon$ |
| $\mathcal{N}(\mu, \sigma)$ | normal distribution with mean $\mu$ and variance $\sigma$ |
| $\varepsilon$ | parameter of the $\varepsilon$-insensitive loss function |
| $\alpha_{i}$ | Lagrange multiplier or expansion coefficient |
| $\beta_{i}$ | Lagrange multiplier |
| $\boldsymbol{\alpha}, \boldsymbol{\beta}$ | vectors of Lagrange multipliers |
| $\xi_{i}$ | slack variables |
| $\xi$ | vector of all slack variables |
| Q | Hessian of a quadratic program |


| $\left\langle\mathbf{x}, \mathbf{x}^{\prime}\right\rangle$ | dot product between $\mathbf{x}$ and $\mathbf{x}^{\prime}$ |
| :---: | :---: |
| $\\|\cdot\\|$ | 2-norm, $\\|\mathbf{x}\\|:=\sqrt{\langle\mathbf{x}, \mathbf{x}\rangle}$ |
| $\\|\cdot\\|_{p}$ | $p$-norm, $\\|x\\|_{p}:=\left(\sum_{i=1}^{N}\left\|x_{i}\right\|^{p}\right)^{1 / p}, N \in \mathbb{N} \cup\{\infty\}$ |
| $\\|\cdot\\|_{\infty}$ | $\infty$-norm , $\\|x\\|_{\infty}:=\max _{i=1}^{N}\left\|x_{i}\right\|$ on $\mathbb{R}^{N},\\|x\\|_{\infty}:=\sup _{i=1}^{\infty}\left\|x_{i}\right\|$ on $\ell_{\infty}$ |
| 1 n | logarithm to base $e$ |
| $\log _{2}$ | logarithm to base 2 |
| $f$ | a function $X \rightarrow \mathbb{R}$ or $X \rightarrow\{ \pm 1\}$ |
| $\mathcal{F}$ | a family of functions |
| $\rho_{f}(x, y)$ | margin of function $f$ on the example ( $x, y$ ), i.e., $y \cdot f(x)$ |
| $\rho_{f}$ | margin of $f$ on the training set, i.e., $\min _{i=1}^{m} \rho_{f}\left(x_{i}, y_{i}\right)$ |
| $h$ | VC dimension |
| C | regularization parameter in front of the empirical risk term |
| $\lambda$ | regularization parameter in front of the regularizer |
| $x \in[a, b]$ | interval $a \leq x \leq b$ |
| $x \in(a, b]$ | interval $a<x \leq b$ |
| $x \in(a, b)$ | interval $a<x<b$ |
| $A^{-1}$ | inverse matrix (in some cases, pseudo-inverse) |
| $A^{\top}$ | transposed matrix (or vector) |
| $A^{*}$ | adjoint matrix (or: operator, vector), |
|  | i.e., transposed and complex conjugate |
| $\left(x_{j}\right)_{j}$ or $\left(x_{j}\right)$ | shorthand for a sequence $\left(x_{j}\right)=\left(x_{1}, x_{2}, \ldots\right)$ |
| $\ell_{p}$ | sequence spaces, $1 \leq p \leq \infty$ (Section B.3.1) |
| $L_{p}(X)$ | function spaces, $1 \leq p \leq \infty$ (Section B.3.1) |
| $I_{A}$ | characteristic (or indicator) function on a set $A$ i.e., $I_{A}(x)=1$ if $x \in A$ and 0 otherwise |
| 1 | unit matrix, or identity map ( $\mathbf{1}(x)=x$ for all $x$ ) |
| \|C| | cardinality of a set $C$ (for finite sets, the number of elements) |
| $\bigcirc$ | regularization operator |
| $\delta_{i j}$ | Kronecker $\delta$ (Section B.2.1) |
| $\delta_{x}$ | Dirac $\delta$, satisfying $\int \delta_{x}(y) f(y) d y=f(x)$ |
| $O(g(n))$ | a function $f(n)$ is said to be $O(g(n))$ if there exists a constant $C$ such that $\|f(n)\| \leq C g(n)$ for all $n$ |
| $o(g(n))$ | a function is said to be $o(g(n))$ if there exists a constant $c$ such that $\|f(n)\| \geq \operatorname{cg}(n)$ for all $n$ |
| rhs/lhs | shorthand for "right/left hand side" |
| - | the end of a proof |
| $\bullet$ | easy problem |
| $\bullet \bullet$ | intermediate problem |
| $\bullet \bullet \bullet$ | difficult problem |
| 000 | open problem |

